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Control of the Input Characteristic and the Displacement Factor of Uni- and Bidirectional SWISS Rectifier for Symmetrical and Unsymmetrical Three-Phase Mains

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Abstract—This paper introduces a phase-oriented control strategy for the uni- and bidirectional three-phase, buck-type SWISS Rectifier. It allows phase shifted sinusoidal input currents which enable the generation of capacitive or inductive reactive power at the converter’s AC grid interface. Furthermore, the operation of the SWISS Rectifier with unsymmetrical AC mains voltages is analyzed. Modifications of the control structure, allowing constant AC input power or ohmic mains behavior even with unsymmetrical AC voltages are presented. Simulations and measurements taken on a 7.5 kW bidirectional SWISS Rectifier hardware prototype demonstrate the validity of the theoretical considerations.

I. INTRODUCTION

The charging of Electric Vehicle batteries requires a conversion of the three-phase AC mains’ voltage into an adjustable DC output voltage level [1]. This is also the case for future LV DC distribution systems and DC micro grids which typically require a connection to the existing AC utility grid [2]. Similar DC distribution systems, with a voltage of ≈400 V DC, are expected to reduce the power consumption and capital cost of data centers and teleco sites by reducing the number of energy conversion stages [3][4].

Typically, if the voltage on the DC bus is lower than the full-rectified AC voltage, two stage systems are used. These consist of a front-end boost type power factor correction (PFC) stage with a 700 V – 800 V DC output connected in series with a DC-DC converter to achieve the desired lower DC bus voltage. For these applications buck-type PFC converters, like the SWISS Rectifier, are an alternative, allowing a single-stage energy conversion between the three-phase mains and a DC bus with lower voltage.

The schematic of the unidirectional SWISS Rectifier, as introduced in [5] and [6], is shown in Fig. 1. It consists of an AC side low-pass input filter, an Input Voltage Selector (IVS), two DC-DC buck converters and a DC output capacitor \( C_{DC} \). Additional capacitors \( C' \) are used to minimize the commutation inductance of the buck converters. The IVS uses a three-phase full-wave diode bridge and a third harmonic injection network to connect the input phase with the converter’s AC grid interface. Further-

A bidirectional extension of the SWISS Rectifier, introduced in [7], is shown in Fig. 2. The additional switches allow a power transfer from the DC to the AC side. In order to enable this feedback of power into the mains the current in the DC-DC converter inductors \( L_n \) and \( L_p \) needs to be reversed. Therefore, switches \( S_{by} \) and \( S_{cy} \) are connected in parallel with the buck converter diodes \( D_{by} \) and \( D_{cy} \) of the unidirectional SWISS Rectifier. Furthermore, the diode bridge of the IVS is extended with six additional switches \( (S_{zk}, S_{kr}, k \in \{a, b, c\}) \) in order to allow it to conduct the reversed currents \( i_{zk} < 0 \) and \( i_{kr} > 0 \). These additional switches are turned on when their antiparallel diode would conduct in the unidirectional SWISS Rectifier. Hence, the switches \( S_{zk}, S_{kr}, S_{bc}, S_{ak}, S_{bd} \) and \( S_{ce} \) are operated at mains frequency.

This paper presents a phase-oriented PWM control method...
for the uni- and bidirectional SWISS Rectifier, which allows the generation of reactive power on the AC side input. It is described in Section II, following an analysis of the topology’s reactive power generation limits. Furthermore analytical formulas for the current stresses of the semiconductors and passive components are derived. Simulation results are included to demonstrate the theoretical considerations. In Section III the operation of the SWISS Rectifier with unsymmetrical mains voltages is analyzed. An extension to the basic control structure is proposed which achieves ohmic behavior at the AC input even with unsymmetrical mains voltages. Section IV presents measurements taken on a 7.5 kW SWISS Rectifier hardware prototype which demonstrates the feasibility of the proposed concepts.

II. OPERATION WITH PHASE SHIFTED AC CURRENTS

As shown in [6], the SWISS Rectifier’s DC-DC converters can be controlled such that the rectifier system’s AC side input currents are sinusoidal and in phase with the grid voltages. This can also be seen from the simplified schematic shown in Fig. 3. By assuming a constant DC output inductor current $I_{DC}$ the local average $\langle i_s \rangle_{T_s}$ of $i_s$ over one switching frequency period $T_s$, can be calculated as

$$\langle i_s \rangle_{T_s} = I_{DC} d_p ,$$

where $d_p$ is the duty cycle of $S_{dp}$. This implies that $d_p$ can be used to control the local average of the input current $i_s$ and hence the current the mains’ phase connected to node $x$ via the IVS. In an analogous way $S_{dn}$ and $d_n$ can be used to control $i_s$. Therefore $d_p$ and $d_n$ can be used to achieve sinusoidal AC input currents and to create reactive power at the system’s AC input by controlling the input displacement factor. However, the generation of reactive power reduces the output voltage range as will be shown in the following.

A. Output Voltage Range

In order to achieve sinusoidal AC side input currents the duty cycle signals $d_p$ and $d_n$ have to be piecewise sinusoidal as described above. Furthermore, the two DC-DC converters create a constant DC output voltage from the three output voltages of the IVS ($u_{PN}, u_{YN}, u_{TN}$),

$$\langle u_{PN} \rangle_{T_s} = u_{PN} (1 - d_p) + u_{PN} d_p ,$$

$$\langle u_{TN} \rangle_{T_s} = u_{TN} (1 - d_n) + u_{TN} d_n ,$$

where $\langle u_{PN} \rangle_{T_s}$ is the local average of $u_{PN}$ over one switching period $T_s$. Note that $\langle u_{PN} \rangle_{T_s}$ is bounded by $u_{PN}$ and $u_{PN}$, while $\langle u_{PN} \rangle_{T_s}$ is bounded by $u_{PN}$ and $u_{TN}$. A drawing of the resulting signals is shown in Fig. 4 a-c).

For ohmic mains behavior the DC output voltage $u_{pn}$ is therefore limited to $1.5 U_1$, where $U_1$ denotes the amplitude of the mains’ phase voltage (cf. Fig. 4 a). Note that the amplitude of the two duty cycle signals ($d_p, d_n$) defines the system’s modulation index $M \in [0; 1]$ which sets the DC output voltage, $u_{pn} = 1.5 U_1$.

If the AC side input currents are phase shifted by the angle $\phi$ (w.r.t. the mains’ phase voltages) this implies that the duty cycle signals have to be shifted as well (cf. Fig. 4 e). Applying the phase shifted $d_p$ and $d_n$ to the input voltages $u_{PN}, u_{YN}$ and $u_{TN}$ results in a reduced output voltage of

$$u_{pn} = \langle u_{PN} \rangle_{T_s} = \frac{3}{2} I_{DC} M \cos(\phi) \quad M \in [0; 1] ,$$

which can also be seen in Fig. 4 d.

B. Reactive Power Generation Limits

In the Fig. 4 d-f the AC side input phase currents are shifted by $\phi = 30^\circ$. Note that either $d_p$ or $d_n$ reaches zero at every mains’ voltage sector boundary (i.e. every $60^\circ$). Any further increase of $\phi$ would result in negative duty cycle values and hence in a low frequency distortion of the AC side input currents. In order to avoid these distortions of the AC input currents, $\phi$ has to be limited to

$$-\frac{\pi}{6} \leq \phi \leq \frac{\pi}{6} .$$

Assuming a constant DC output current $I_{DC}$ and neglecting any losses in the semiconductors and filter components the active and reactive power at the converter’s mains interface can be derived as

$$P = \frac{3}{2} U_1 I_{DC} M \cos(\phi) = S_{\max} M \cos(\phi) ,$$

$$Q = \frac{3}{2} U_1 I_{DC} M \sin(\phi) = S_{\max} M \sin(\phi) .$$

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This leads to the reactive power generation limits shown in Fig. 5. Note that the same reactive power generation limits exist for the six-switch buck-type PWM converter [8].

C. Control Structure

The phase voltage oriented control structure shown in Fig. 6 allows the generation of reactive power on the rectifier’s AC side using the considerations given above. As in [5] An outer loop voltage controller $R(s)$ is used in order to control the DC output voltage $u_{\text{DC}}$ by creating a reference signal $i_{\text{DC}}^*$ for the underlying current controller $G(s)$. The output voltage reference $u_{\text{DC}}^*$ is added as a feedforward signal to the current controller’s output to calculate the DC-DC converter output voltage reference $u_{\text{DC}}$. Dividing by the maximum DC voltage $(1.5 U_1 \cos(\phi))$, cf. (4)) yields the modulation index $M$. In order to achieve sinusoidal AC input currents, $M$ is multiplied with piecewise sinusoidal, unity amplitude shaping signals $s_p$ and $s_n$. An illustration of these signals (for $\phi = 30^\circ$) is shown in Fig. 7. The signals $s_p$ and $s_n$ are calculated as weighted sum from the corresponding shaping signals for ohmic behavior ($s_{\text{on}}$, $s_{\text{on}}$) and a signal leading by $90^\circ$ ($s_{\text{on}}$, $s_{\text{on}}$) as shown in Fig. 6. This control structure ensures that the duty cycle signals $d_a$ and $d_b$ will not exceed the converter’s linear operating range given conditions (4) and (5) are met.

Figure 8 shows simulation results for a 7.5 kW SWISS Rectifier with key parameters as listed in Table I. For the first 20 ms the rectifier operates with $\phi = -30^\circ$ which results in inductive behavior. From $t = 20$ ms to $t = 40$ ms no phase shift is applied ($\phi = 0^\circ$) which results in AC currents which are in phase with the phase voltages. For $t > 40$ ms the AC currents lead the voltage ($\phi = 30^\circ$), which results in capacitive behavior. Simulation results for the same system, but with DC-to-AC power transfer, are shown in Fig. 9. Again, the converter can be operated with a phase shift of up to $\phi = \pm 30^\circ$ with sinusoidal input currents. This allows the generation of reactive power on the AC side, which e.g. could be used to compensate the reactive power demand of the AC grid filter. For example, a similar approach as presented in [9] for the six switch rectifier could be used.

<table>
<thead>
<tr>
<th>Table I: Specifications of Simulated SWISS Rectifier</th>
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<tr>
<td>AC Input Voltage (Line to Neutral)</td>
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<td>AC Input Frequency</td>
</tr>
<tr>
<td>Switching Frequency</td>
</tr>
<tr>
<td>Nominal DC Voltage</td>
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<tr>
<td>DC Link Capacitor</td>
</tr>
<tr>
<td>DC Link Inductor</td>
</tr>
<tr>
<td>DC Output Power</td>
</tr>
<tr>
<td>AC Filter Inductor</td>
</tr>
<tr>
<td>AC Filter Capacitor</td>
</tr>
</tbody>
</table>

Fig. 8. Simulated mains voltages $u_{\text{abc}}$, input currents $i_{\text{abc}}$, and DC-DC converter duty cycles $d_a$ and $d_b$ for $\phi = -30^\circ$ (inductive), $\phi = 0^\circ$ (ohmic) and $\phi = 30^\circ$ (capacitive) AC side currents for AC-to-DC power transfer.
Fig. 9. Simulated grid voltages $u_{a,b,c}$, input currents $i_{a,b,c}$ and DC-DC converter duty cycles $d_p$ and $d_n$ for $\phi = -30^\circ$ (capacitive), $\phi = 0^\circ$ (ohmic) and $\phi = 30^\circ$ (inductive) AC side currents for DC-to-AC power transfer.

D. Current Stresses

In order to select components for a SWISS Rectifier design the current stresses of the passive components and the semiconductor devices have to be calculated. This section extends the analytical equations presented in [6] for phase shifted AC input currents. The following analysis assumes AC-to-DC power transfer, however, analog equations can be derived for DC-to-AC power transfer as well. Furthermore, any switching frequency ripple in the DC side filter inductors $L_p$ and $L_n$ and in the AC side filter inductors $L_f$ is neglected.

1) DC-DC Converters: In AC-to-DC power transfer only the switches $S_{xp}$ and $S_{nz}$ and the diodes $D_{yp}$ and $D_{ny}$ conduct current. The switch $S_{xp}$ conducts the DC output current $I_{DC}$ when it is turned on while the diode $D_{yp}$ conducts while $S_{xp}$ is off. Neglecting the output current’s switching frequency ripple this can be expressed as

$$i_{xp} = \begin{cases} I_{DC} & \text{if } S_{xp} \text{ is on} \\ 0 & \text{if } S_{xp} \text{ is off} \end{cases}$$

$$i_{yp} = I_{DC} - i_{xp}. \quad (8)$$

In order to calculate the rms and average current of the DC-DC converter semiconductors the duty cycle $d_p$ of $S_{xp}$ is required. Using Fig. 6 the positive side duty cycle can be derived as

$$d_p(\omega t) = M [\cos(\phi) \cos(\omega t) - \sin(\phi) \sin(\omega t)] \quad (9)$$

$$\text{for } -\frac{\pi}{3} \leq \omega t \leq \frac{\pi}{3}. \quad (10)$$

Using (8) the rms current conducted by $S_{xp}$ can be calculated as

$$I_{xp,\text{rms}} = I_{DC} \sqrt{\frac{3\sqrt{3}}{2\pi} M_d} \quad \forall \phi \in \left[\frac{\pi}{6}, \frac{\pi}{6}\right]. \quad (12)$$

where $M_d$ denotes the active power modulation index, defined as

$$M_d = M \cos(\phi) = \frac{P}{S_{\text{max}}}. \quad (13)$$

Similarly the average current in $S_{xp}$ can be found by integration as

$$I_{xp,\text{avg}} = I_{DC} \sqrt{\frac{3\sqrt{3}}{2\pi} M_d} \quad \forall \phi \in \left[\frac{\pi}{6}, \frac{\pi}{6}\right]. \quad (14)$$

As the diode $D_{yp}$ conducts the DC current $I_{DC}$ whenever $S_{xp}$ is turned off its rms and average current can directly be derived using (12) and (14),

$$I_{yp,\text{rms}} = I_{DC} \sqrt{1 - \frac{3\sqrt{3}}{2\pi} M_d} \quad \forall \phi \in \left[\frac{\pi}{6}, \frac{\pi}{6}\right]. \quad (15)$$

$$I_{yp,\text{avg}} = I_{DC} \left(1 - \frac{3\sqrt{3}}{2\pi} M_d\right) \quad \forall \phi \in \left[\frac{\pi}{6}, \frac{\pi}{6}\right]. \quad (16)$$

Due to the symmetry of the positive and the negative side DC-DC converters the same current stresses result for $S_{nx}$ and $D_{ny}$.

Note that the rms and average currents in the DC-DC converter switches and diodes do not depend directly on $\phi$ but are a function of the active power $P$. This implies that the current stresses, and hence the conduction losses, in the DC-DC converter semiconductors are typically independent of the reactive power $Q$ generated on the AC side. As the DC-DC converter switching losses depend on the input voltages $u_{xy}$, $u_{yz}$ and the DC side output current $I_{DC}$ they do not depend on $Q$ either. Hence only active power is processed by the DC-DC converters.

2) IVS: As can be seen from the schematic shown in Fig. 1 exactly one of the three positive side rectifier diodes ($D_{xa}$, $D_{xb}$, $D_{xc}$) is conducting during each grid voltage sector. Therefore, the forward biased diode conducts the same current as the switch $S_{xp}$. The rms and average current stress of the rectifier diodes can then be calculated using (12) and (14),

$$I_{dxk,\text{rms}} = I_{DC} \sqrt{\frac{\sqrt{3}}{2\pi} M_d} \quad \forall k \in \{a, b, c\}. \quad (17)$$

$$I_{dxk,\text{avg}} = I_{DC} \frac{\sqrt{3}}{2\pi} M_d \quad \forall k \in \{a, b, c\}. \quad (18)$$

Due to the circuit’s symmetry the same equations result for the negative side diodes $D_{za}$, $D_{zb}$, $D_{zc}$.

In the third harmonic injection network exactly one of the three four-quadrant switches $S_{xya}$, $S_{yby}$, $S_{ycy}$ is turned on during each grid voltage sector. Furthermore, the injection current $i_x$ flows through one active switch and one diode of the turned-on four-quadrant switch. Which one of the two active switches and diodes is conducting depends on the sign of $i_x$. The same rms and average current stresses result for all four semiconductors of each four-quadrant switch due to phase symmetry. Considering only $i_x > 0$ and the grid voltage sectors where $S_{xya}$ is on $(\pi/3 < \omega t < 2\pi/3)$ and $4\pi/3 < \omega t < 5\pi/3$ the current in $S_{xya}$ can be expressed as

$$i_{xya} = \begin{cases} I_{DC} & \text{if } d_n > d_p \\ 0 & \text{otherwise} \end{cases} \quad (19)$$
The rms and average current stresses can then be found by integration

\[ I_{\text{Skyk}, \text{rms}} = I_{\text{DC}} \sqrt{\frac{M_\phi}{\pi} \left[ \frac{1}{\cos(\phi)} - \frac{\sqrt{3}}{2} \right]} \quad \forall k \in \{a, b, c\}, \]

\[ I_{\text{Skyk}, \text{avg}} = I_{\text{DC}} \sqrt{\frac{M_\phi}{\pi} \left[ \frac{1}{\cos(\phi)} - \frac{\sqrt{3}}{2} \right]} \quad \forall k \in \{a, b, c\}. \]

If no reactive power is generated (\( \phi = 0^\circ \)), the average current stress of the injection network switches \( S_{\text{Skyk}} \) is \( \approx 15\% \) of the average current stress of the rectifier diodes \( D_{kx} \) and \( D_{ak} \). The same value results for the ratio of squared rms currents. This implies that the conduction losses in the injection network switches \( S_{\text{Skyk}} \) will typically be considerably lower than conduction losses in the rectifier diodes \( D_{kx} \), \( D_{ak} \) and corresponding parallel switches \( S_{zk} \) and \( S_{zk} \).

Note that the rms and average current in the current injection network increase with the absolute value of the phase shift angle \( \phi \). The maximum rms current, occurring for \( \phi = \pm 30^\circ \), is \( \approx 47\% \) higher compared to \( \phi = 0^\circ \) while the average current current is \( \approx 115\% \) higher. Therefore, the conduction losses in the injection network at \( \phi = \pm 30^\circ \) are \( \approx 2.15 \) times the losses if no reactive power (\( \phi = 0^\circ \)) is generated.

3) Passive Components: As shown above, the generation of the reactive power on the AC side does not influence the active power transferred to the DC side directly. Therefore, the current and voltage stresses of the buck converter inductors (\( L_p, L_n \)) and the output capacitor (\( C_{pn} \)) are almost independent of the reactive power generated on the AC side. Note that the AC side input currents \( i_a, i_b, i_c \) depend only on the modulation index \( M \) but not on the actual phase shift angle \( \phi \), as can be seen from Fig. 4:

\[ I_{a,b,c} = \frac{I_{\text{DC}}}{\sqrt{2}} \leq \frac{I_{\text{DC}}}{\sqrt{2}}. \]

Finally the rms current stress of the AC side input filter capacitors can be calculated from the equations derived above. During each grid voltage vector either one of the rectifier diodes \( D_{kx}, D_{ak} \) or the injection switch \( S_{zk} \) is conducting. Therefore the corresponding rms currents can be combined using Pythagorean addition (cf. Fig. 10, \( k = a, k = a \))

\[ I_{\text{Crms}} = \sqrt{I^2_{\text{Dx}, \text{rms}} + I^2_{\text{Dx}, \text{rms}} + 2I^2_{\text{Skyk}, \text{rms}} - I^2_k}. \]

\[ = I_{\text{DC}} \sqrt{\frac{2}{\pi} M - \frac{1}{2} M^2}. \]

It can be seen that the filter capacitor’s rms current stress depends on the modulation index \( M \in [0; 1] \) but not on the phase shift angle \( \phi \). The highest rms current stress, which is typically required for the dimensioning of a rectifier system, can be calculated as

\[ I_{\text{Crms}}(M) \leq I_{\text{DC}} \sqrt{\frac{2}{\pi}} \approx 0.45 I_{\text{DC}}. \]

4) Numerical Results: In Table II numerical simulation results for the rms and average current stresses are compared to the corresponding values calculated using the analytical equations derived above. Two operating points, one with purely active power (\( \phi = 0^\circ \)) and one with maximum reactive power (\( \phi = 30^\circ \)) are shown. In both cases the deviation between value calculated with the analytical formula and the simulation result is less than \( 3.4\% \). Accordingly, the analytical expressions can directly be used for dimensioning the system.

### Table II

<table>
<thead>
<tr>
<th>( \phi )</th>
<th>Calculation</th>
<th>Simulation</th>
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<td>0°</td>
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<tr>
<td>M</td>
<td>83.3%</td>
<td>87.9%</td>
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<td>12.9 A</td>
<td>12.9 A</td>
<td>-0.1%</td>
<td></td>
</tr>
<tr>
<td>10.5 A</td>
<td>10.4 A</td>
<td>0.3%</td>
<td></td>
</tr>
<tr>
<td>10.5 A</td>
<td>10.4 A</td>
<td>0.3%</td>
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<td>7.26 A</td>
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</table>

### III. Operation with Unsymmetric Mains Voltages

So far, the AC grid voltages were assumed to be purely sinusoidal, of equal amplitude and shifted by 120°. However, real AC distribution grids typically exhibit several percent of low frequency harmonics and an asymmetry of the phase voltages. In this section control strategies for constant output power and resistive mains behavior are analyzed.

#### A. Constant Power Transfer

It can be seen from the schematic shown in Fig. 6 that the power transferred to the rectifier’s DC output is given by

\[ p_{\text{DC}}(t) = u_{\text{pn}}(t) i_{\text{DC}}(t). \]

If the output voltage controller \( R(s) \) and the current controller \( G(s) \) have settled, \( p_{\text{DC}} \) will be constant for stationary
operation and constant load. Furthermore, the power delivered to the DC bus is almost independent of the AC grid voltages in this case. Hence, this control scheme allows an operation of the converter with the minimal DC output filter capacitance $C_{pp}$. The power drawn from the AC grid by the SWISS Rectifier is given by equation (27). If losses in the converter are neglected, the power drawn from the AC grid has to be equal to the power delivered to the DC output, as the Input Voltage Selector and the DC-DC converters contain only switching frequency energy storage elements.

$$p_{AC}(t) = u_a(t) i_a(t) + u_b(t) i_b(t) + u_c(t) i_c(t)$$

(27)

$$p_{AC}(t) = p_{DC}(t) = p(t)$$

(28)

If the AC grid voltages $u_{a,b,c}$ are asymmetrical, e.g. if the amplitudes of the individual phase voltages are not equal, constant AC side power $p_{AC} = p_{DC}$ can only be achieved with non-sinusoidal grid currents $i_{a,b,c}$.

### B. Constant Input Resistance

In certain applications the rectifier system might be required to behave like a symmetrical resistive load even with unsymmetrical grid voltages. In this case the AC side input currents $i_{a,b,c}$ are given by equation (29). $R_{in}$ is the resistance of one phase of a fundamental frequency rectifier equivalent circuit for star connection. Note that, since the converter has no connection to the AC grid’s neutral $N$, no zero sequence current $i_0 = (i_a + i_b + i_c)/3$ can be created by the rectifier. Therefore only the positive and negative sequence components $u'_{a,b,c}$ of the grid voltages $u_1$ contribute to the power flow and hence equation (30) results.

$$i_k(t) = \frac{u_k(t)}{R_{in}} \quad \forall k \in \{a, b, c\}$$

(29)

$$p_{AC}(t) = \frac{1}{R_{in}} \left[ u'^2_a(t) + u'^2_b(t) + u'^2_c(t) \right]$$

(30)

Due do the balance of power on the AC and DC side of the converter and equation (26), the DC side output current $i_{DC}(t)$ has to be proportional to $p_{AC}(t)$. This can be achieved with the control structure shown in Fig. 11. The output signal $I_{DC}^{*}$ of the DC voltage controller $R(s)$ is multiplied with a shaping signal $m$ in order to derive the DC link current reference for the current controller. No changes are required to the current control loop shown in Fig. 6. The signal $m$ is calculated by subtracting the zero sequence system of the measured input voltages $u_{a,b,c}$ and summing their squares. A scaling factor of $2/3U_{1, pos}^2$ is used, where $U_{1, pos}$ is the amplitude of the first harmonic positive sequence system. This ensures $m = 1$ for symmetrical phase voltages with nominal amplitude $U_1 = U_{1, pos}$.

In Fig. 12 simulation results are shown for the SWISS Rectifier specified in Table I, operated at a AC grid where the voltage amplitude of phase $a$ is 23 V higher than on phases $b$ and $c$. Until $t = 30$ ms the converter operates with the control structure shown in Fig. 6 (i.e. $m = 1$), causing low frequency distortions of the input currents due to the constant instantaneous power flow requirement. At $t = 30$ ms the control system is changed to the structure shown in Fig. 11. Therefore, the AC side input currents are now sinusoidal and $i_a$ has a higher amplitude than $i_b$ and $i_c$ as expected from (29). Furthermore the DC current reference signal $i_{DC}^{*}$ is no longer constant due to the instantaneous power flow pulsating with twice the mains frequency.

### IV. IMPLEMENTATION RESULTS

A SWISS Rectifier prototype has been built according to the specifications given in Table I, a picture of the prototype hardware is shown in Fig. 14. The values of all major components match those used for creating the simulation results shown in the previous sections. Measurements taken on this prototype are presented in the following.

#### A. Phase Shifted AC Currents

Figure 15 shows measurement results for AC-to-DC power transfer at 7.3 kW DC output power. Note that the
voltage and current of phases a and b where measured directly while the quantities for phase c were recreated assuming \( u_a + u_b + u_c = 0 \) and \( i_a + i_b + i_c = 0 \). During the first grid voltage period \((0 < t < 20 \text{ ms})\) the converter is operated with a phase shift of \(\phi = -30^\circ\) resulting in inductive behavior. At \(t = 20 \text{ ms}\) the phase shift angle \(\phi\) is set to zero resulting in almost purely active power drawn from the AC grid. The remaining capacitive reactive power is caused by the input filter. Finally \(\phi\) is set to \(30^\circ\) at \(t = 40 \text{ ms}\) resulting in capacitive behavior in the third grid voltage period shown.

The same sequence of input current phase angle steps as described above has been applied for DC-to-AC power transfer (7.5 kW) in the measurement shown in Fig. 16. For both, AC-to-DC and DC-to-AC power transfer, sinusoidal AC side currents result for all tested values of \(\phi\).

### B. Operation Under Unsymmetrical Mains Voltages

In order to test the operation of the SWISS Rectifier under unsymmetrical AC grid voltages the control structure proposed in Section III is implemented. A three-phase grid containing a first harmonic negative sequence voltage component with an amplitude of 19 V is used for the measurements. Note that no DC output voltage controller was used, the DC voltage \(u_{\text{D}}\) was defined by a constant voltage source (or sink) instead.

Measurement results for AC-to-DC power transfer are shown in Fig. 17. During the first 30 ms the converter is operated with constant AC side input power resulting in non-sinusoidal grid currents \(i_{a,b,c}\). At \(t = 30 \text{ ms}\) the control
the mains’ phase voltages. This allows the generation of reactive power under certain conditions. However, the generation of reactive power reduces the output voltage range of the rectifier system.

Furthermore, analytical equations for the resulting rms and average current stresses of the converter’s switches and passive components are derived for reactive power generation. The resulting formulas show that the rms current stress in the injection network’s four quadrant switches increases from 0.21 \( I_{DC} \) if no reactive power is generated to 0.30 \( I_{DC} \) at \( \phi = 30^\circ \). The corresponding average current stress increases from 0.04 \( I_{DC} \) to 0.09 \( I_{DC} \). The conduction and switching losses of all other semiconductors, including the IVS’ full wave diode bridge, are not affected by the generation of reactive power.

Additionally, the operation of a SWISS Rectifier with un-symmetrical mains voltages has been analyzed. A proposed structure of the control improves the SWISS Rectifier to achieve ohmic mains behavior or constant power transfer even if the AC input voltages are unbalanced.

Simulations and measurements taken on a 7.5 kW laboratory prototype SWISS Rectifier demonstrate the feasibility of the proposed concepts.

**ACKNOWLEDGMENT**

The authors would like to thank ABB Switzerland Ltd. for the funding and for their support regarding many aspects of this research project.

**REFERENCES**


